

Symbolic Reachability Graph



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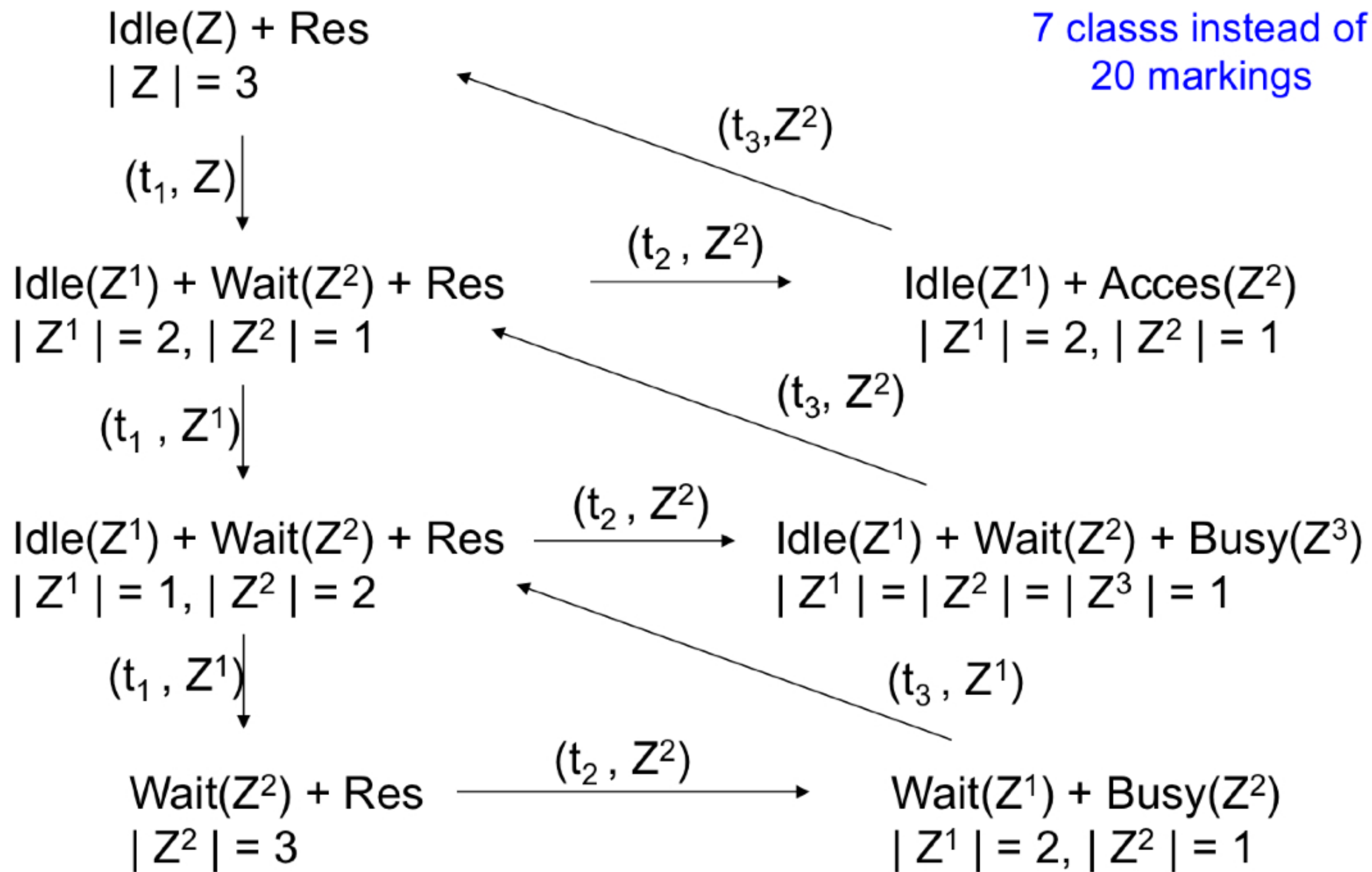
We are ready to derive an algorithm to construct the symbolic reachability graph.

SRG construction Algorithm

```
SRG_Construction( $N = \langle P, T, C, W^-, W^+, M_0 \rangle$ )  
   $SRG.Q = \{\hat{M}_0\}$ ;  $SRG.\delta = \emptyset$ ;  
   $SRG.q_0 = \hat{M}_0$ ;  $sStates = \{\hat{M}_0\}$ ;  
  While ( $sStates \neq \emptyset$ ) {  
     $\hat{s} =$  pick a sstate in  $sStates$  ;  
     $sStates = sStates \setminus \{\hat{s}\}$ ;  
    for each  $t \in T, \hat{c} \in \hat{C}(t)$  {  
      if ( $\hat{s}[(t, \hat{c})]$ ) {  
         $\hat{s}[(t, \hat{c})] \hat{n}s$ ;  
        if ( $\hat{n}s \notin SRG.Q$ ) {  
           $SRG.Q = SRG.Q \cup \{\hat{n}s\}$  ;  
           $sStates = sStates \cup \{\hat{n}s\}$ ;  
        }  
         $SRG.\delta = SRG.\delta \cup \{(\hat{s}, \hat{n}s)\}$ ;  
         $SRG.\lambda(\hat{s}, \hat{n}s) = (t, \hat{c})$ ;  
      }  
    }  
  }  
return  $SRG$ ;
```

Example: SRG of the critical section access model

7 classes instead of 20 markings



Example: SRG of the dining philosophers problem

Think(Z) + F(Z)

| Z | = 5

(TF, Z)

(PF, Z²)

Think(Z¹+Z³) + F(Z¹) + Eat(Z²)

| Z¹ | = 3, | Z² | = | Z³ | = 1

(TF, Z^{1,0}),

(TF, Z^{1,1})

(PF, Z¹),

(PF, Z⁴)

Think(Z²+ Z³+ Z⁵) + F(Z³) + Eat(Z¹+ Z⁴)

| Zⁱ | = 1

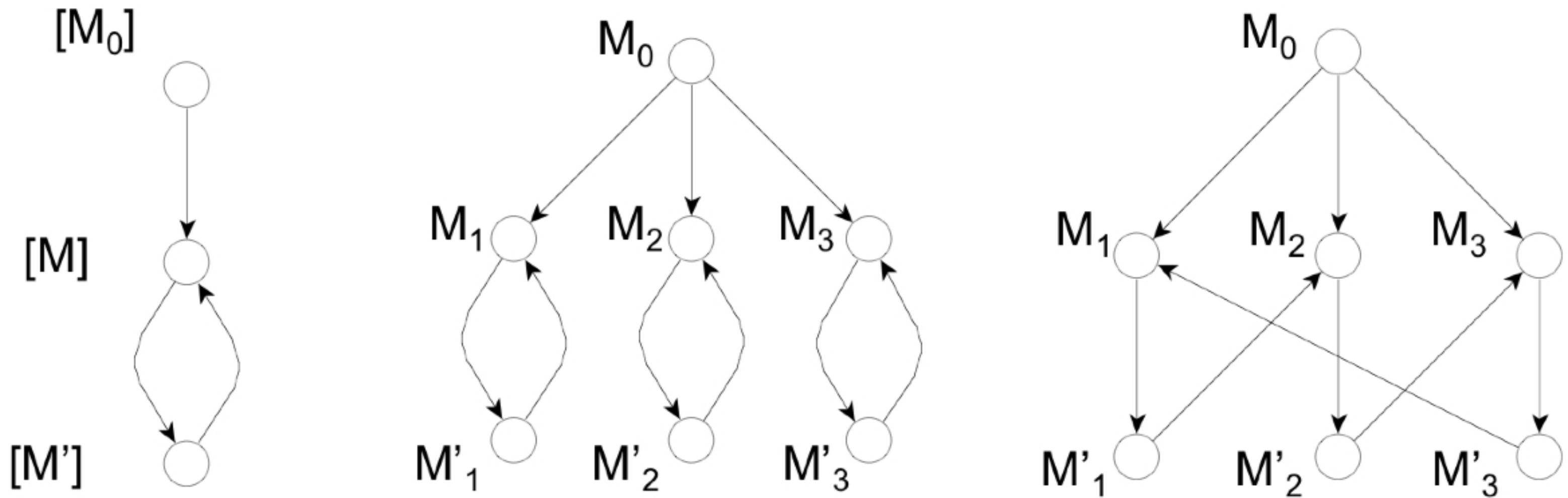
3 symbolic markings instead of 11 markings

What does the Symbolic Reachability Graph preserve?

- Each marking represented by a class (a symbolic marking) is reachable.
- Each reachable marking is represented by a class.
- Each firing sequence of the RG is represented in the SRG.
- To each sequence of the symbolic graph corresponds a sequence of the RG.

Then, what is missing?

- We cannot distinguish the following situations:



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 - ▶ A class groups a set of objects that have the same nature.
 - ▶ The obtained reduction, SRG vs. RG, is maximal.
- How to deal with the case where objects have the same nature, *but with potentially different behaviours?*
 - ▶ Example: a class that represents a set of processors divided in two subsets: fast and slow.

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 - ▶ Example: a class that represents a set of processors divided in two subsets: fast and slow.
- Use of static subclasses...
 - ▶ Each class is partitioned into cells, called static subclasses, where the objects of the same cell behave identically.
 - ▶ Symmetries of net extends easily as follows... (next sequence)